

component of the field can have a specific temporal correlation and, thus, *coherence time*, $\tau_c(\mathbf{k}_\perp) = 1/\Delta\omega(\mathbf{k}_\perp)$. Conversely, each monochromatic component can have a particular spatial correlation and, thus, *coherence area*, $A_c(\omega) = 1/\Delta k^2(\omega)$.

The two variances can be further *averaged* with respect to these variables, such that they become constant,

$$\langle \Delta\omega^2 \rangle_{k_\perp} = \frac{\int_{A_{k_\perp}=-\infty}^{\infty} \int_{-\infty}^{\infty} (\omega - \langle \omega \rangle)^2 S(\mathbf{k}_\perp, \omega) d\omega d^2\mathbf{k}_\perp}{\int_{A_{k_\perp}=-\infty}^{\infty} \int_{-\infty}^{\infty} S(\mathbf{k}_\perp, \omega) d\omega d^2\mathbf{k}_\perp}, \quad (39a)$$

$$\langle \Delta k_x^2 \rangle_\omega = \frac{\int_{-\infty}^{\infty} \int_{A_{k_\perp}=-\infty}^{\infty} (k_x - \langle k_x \rangle)^2 S(\mathbf{k}_\perp, \omega) d^2\mathbf{k}_\perp d\omega}{\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} S(\mathbf{k}_\perp, \omega) d^2\mathbf{k}_\perp d\omega}. \quad (39b)$$

Equation (39a) yields a coherence time, $\tau_c = 1/\sqrt{\langle \Delta\omega^2 \rangle}$, that is averaged over all spatial frequencies, while Eq. (39b) provides a coherence area, $A_c = 1/\langle \Delta k_x^2 \rangle$, which is averaged over all temporal frequencies. In practice, we always deal with fields that fluctuate in both time and space, but rarely do we specify τ_c as a function of \mathbf{k} or vice-versa; we implicitly assume averaging of the form in Eq. (39a) and (39b).

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